

Chapter 7 Notes

SAMPLING DISTRIBUTION:		
Definition: The distribution of the statistic from every possible sample of size n .	Example: Proportion of students in band	Population: Harbor high students
	Sample Size: $n = 12$	
	Describe (what does one dot represent?): The proportion of students in band from a random sample of 12 harbor students.	

A number that describes the whole **population** is known as a parameter.

A number that is calculated from a **sample** is known as a statistic.

We always use a statistic to estimate a parameter.

In Section 7.2, we used a sample proportion to estimate a population proportion.

In Section 7.3, we used a sample mean to estimate a population mean.

	Sample Proportions	Sample Means	SD
What is the parameter?	P	M	σ
What is the statistic?	\hat{p}	\bar{x}	S
Draw Sampling Distribution. (if Normal)	<p>Sampling Distribution of \hat{p}</p>	<p>Sampling Distribution of \bar{x}</p>	
When is the sampling distribution approximately normal?	Large Counts! $np \geq 10$ $n(1-p) \geq 10$	<ul style="list-style-type: none"> Pop. Dist. is approx. Normal OR C.L.T. $\rightarrow n \geq 30$ 	
What is the mean of the sampling distribution?	$M_{\hat{p}} = P$	$M_{\bar{x}} = M$	

	Sample Proportions	Sample Means
What is the standard deviation of the sampling distribution?	$\sigma_{\hat{p}} = \sqrt{\frac{P(1-P)}{n}}$	$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$
What condition must be satisfied in order to use the above formula?	10% condition! $n \leq \frac{1}{10} N$	10% condition! $n \leq \frac{1}{10} N$
What is the formula for a z-score?	$z = \frac{\hat{p} - P}{\sqrt{\frac{P(1-P)}{n}}}$	$z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}}$

Old stuff from Chapter 6:

Binomial Distributions	
B: BINARY! Outcomes can be categorized as "success" or "failure"	Formula for Binomial Probabilities: $P(x=k) = {}_n C_k (p)^k (1-p)^{(n-k)}$ <div style="display: flex; justify-content: space-between; align-items: center;"> <div> <p>n = # of trials k = desired # of successes p = probability of success</p> </div> <div style="border: 1px solid black; border-radius: 50%; padding: 10px; text-align: center;"> <p>COMBINATIONS</p> <p>$\binom{n}{k}$ is same as ${}_n C_k$</p> </div> </div>
I: Independent OR "10% Condition" <div style="font-size: small;"> <p>one trial doesn't affect the next $\rightarrow np \geq 10$ and $(n)(1-p) \geq 10$</p> </div>	
N: Set NUMBER of trials. $n = \underline{\hspace{2cm}}$	
S: SAME probability for all trials $p = \underline{\hspace{2cm}}$	
Mean of a Binomial Distribution: $\mu = np$	The following situation might be tricky: $N = 152$ "Ms. Ramer will randomly choose 15 of her 152 students to attend the state math fair. Julian is hoping that he and a few of his friends will be chosen to go. (He considers 10 of Ms. Ramer's students to be his good friends.) Given that Julian is one of the chosen students, what is the probability that at least two of his friends will also be chosen."
Standard Deviation of a Binomial Distribution: $\sigma = \sqrt{np(1-p)}$	If Julian is chosen, there are 14 more people Explain why this situation is a binomial probability to be setting: B success = friend chosen failure = not friend <div style="display: flex; align-items: center;"> <div style="margin-right: 20px;"> <p>1 $(14) \left(\frac{10}{151}\right) \geq 10$ is not</p> </div> <div> <p>and $(14) \left(\frac{141}{151}\right) \geq 10$</p> </div> </div> <div style="margin-left: 20px; font-size: small;"> <p>chosen and 151 people to choose from.</p> </div>
Shape of a Binomial Distribution (Normal if...): Large Counts! $np \geq 10$ AND $n(1-p) \geq 10$	N $n = 14$ S $p = \frac{10}{151}$ <div style="text-align: right;"> <p>Whoops! Not Binomial because of independence.</p> </div>

$P(x \geq 2)$